

Simplify Each of the Following (Basic Skills)

$$1. -22 + (-15) - 1 =$$

$$\underline{-22 - 15 - 1}$$

$$\underline{-38}$$

1. -38

$$2. 8 - (-7) + 3 =$$

$$\underline{8 + 7 + 3}$$

$$\underline{18}$$

2. 18

$$3. 2 - (-8) - 11 =$$

$$\underline{2 + 8 - 11}$$

$$\underline{10 - 11}$$

$$\underline{-1}$$

3. -1

$$4. 9 \cdot (-3) \cdot 0 \cdot 7 =$$

$$\underline{0}$$

4. 0

$$5. 5 \cdot (-3) \cdot (-2) \cdot (-3) =$$

$$\underline{-15 \cdot (-2) \cdot (-3)}$$

$$\underline{30 \cdot (-3)}$$

$$\underline{-90}$$

5. -90

$$6. -7 \frac{3}{11} + -2 \frac{6}{11} - 1 \frac{6}{11} =$$

6. $-8 \frac{3}{11}$

$$\underline{-7 - 2 + 1} \quad \underline{-3 - 6 + 6}$$

$$\underline{-8} \quad \underline{-3}$$

$$\underline{-8 \frac{3}{11}}$$

$$7. \frac{-2}{3} - \frac{4}{12} + \frac{7}{24} =$$

7. $-17/24$

$$\underline{\frac{-16}{24} \quad \frac{-8}{24} \quad \frac{+7}{24}}$$

$$\underline{= -17/24}$$

$$8. \frac{-3}{8} + 2 \frac{2}{5} - 2 \frac{3}{4} =$$

8. $-29/40$

$$\underline{2 - 2} \quad \underline{\frac{-15}{40} \quad \frac{16}{40} \quad \frac{-30}{40}} = \underline{-29/40}$$

$$9. -3 \frac{1}{5} \cdot 1 \frac{1}{5} \div -\frac{2}{5} =$$

9. $+9 \frac{3}{5}$

$$\underline{\frac{-16}{5} \cdot \frac{6}{5} \cdot \frac{-5}{2}} = \underline{\frac{-48}{5} = +9 \frac{3}{5}}$$

$$10. -2 \frac{1}{5} \div 3 \frac{1}{2} \cdot \frac{1}{3} =$$

10. $-22/105$

$$\underline{-\frac{11}{5} \cdot \frac{2}{7} \cdot \frac{1}{3}} = \underline{\frac{-22}{105}}$$

Order of Operations

$$11. \left(\frac{3-2}{4-3}\right)^2 \div \frac{7}{12} - \frac{1}{2} \cdot \frac{1}{6}$$

$$\left(\frac{9-8}{12}\right)^2 \cdot \frac{12}{7} - \frac{1}{2} \cdot \frac{1}{6}$$

$$\left(\frac{1}{12}\right)^2 \cdot \frac{12}{7} - \frac{1}{12}$$

$$\frac{1}{144} \cdot \frac{12}{7} - \frac{1}{12}$$

$$\frac{1}{12} \cdot \frac{1}{7} - \frac{1}{12}$$

$$\frac{1}{84} - \frac{7}{84}$$

$$\frac{-6}{84} = -\frac{1}{14}$$

11. -1/14

$$12. \frac{2}{3}[5(7-5)^2 + (3 \cdot 2) + 2^2 - 1]$$

$$\frac{2}{3}[5(2)^2 + 6 + 4 - 1]$$

$$\frac{2}{3}[5(4) + 6 + 4 - 1]$$

$$\frac{2}{3}[20 + 6 + 4 - 1]$$

$$\frac{2}{3}(29)$$

$$\frac{58}{3} = 19\frac{1}{3}$$

12. 19 1/3

Properties and Identities

Match each of the following and watch out for bad examples

13. G commutativity over multiplication

A. $4k + 5 = 4k + 5$ REFLEXIVE

14. B associativity of multiplication

B. $7 \cdot (2 \cdot 1) = (7 \cdot 2) \cdot 1$ ASSOC. MULT.

15. D additive identity

C. If $3(5) = 11 + 4$ and $11 + 4 = 15$
then $3(5) = 15$ TRANSITIVE

16. A reflexive property

D. $X + 0 = X$ ADDITIVE IDENT

17. H distributive prop. from left over addition

E. $4 + (-4) = 0$ ADDITIVE INVERS

18. C transitive property

F. $8 + (-8) = 17$ FALSE STATEMENT

19. E additive inverse

G. $M \cdot K + 5 = K \cdot M + 5$ COMMUTATIVE MULT

H. $3(5x + 2) = 15x + 6$ DIST FROM LEFT OVER ADD

I. If $y + 7 = 11$ then $11 = y + 7$ SYMMETRIC

Solve each equation

32. $\left[\frac{5r-2}{-3}=4\right] \cdot -3$

$$\begin{aligned}5r-2 &= -12 \\5r &= -12+2 \\ \frac{5r}{5} &= \frac{-10}{5} \\ r &= -2\end{aligned}$$

32 _____

33. $3m+2=23$

$$\begin{aligned}3m &= 23-2 \\ \frac{3m}{3} &= \frac{21}{3} \\ m &= 7\end{aligned}$$

33 _____

34. $9m-5=67$

$$\begin{aligned}9m &= 67+5 \\ \frac{9m}{9} &= \frac{72}{9} \\ m &= 8\end{aligned}$$

34 _____

35. $\frac{k}{-2}-3=4$

$$\begin{aligned}\frac{k}{-2} &= 4+3 \\ -2\left[\frac{k}{-2}=7\right] \\ k &= -14\end{aligned}$$

35 _____

36. $\left[-7=\frac{4f-5}{3}\right] 3$

$$\begin{aligned}-21 &= 4f-5 \\ -21+5 &= 4f \\ -16 &= 4f \\ -4 &= f\end{aligned}$$

36 _____

37. $6(7-3w)=5w-2$

$$\begin{aligned}42-18w &= 5w-2 \\ 42+2 &= 5w+18w \\ \frac{44}{23} &= \frac{23w}{23} \\ 1\frac{21}{23} &= w\end{aligned}$$

37 _____

38. $2(7z+3)-6=2(z-5)+4z$

$$\begin{aligned}14z+6-6 &= 2z-10+4z \\ 14z &= 6z-10 \\ 14z-6z &= -10 \\ \frac{8z}{8} &= \frac{-10}{8} \\ z &= -1\frac{1}{4}\end{aligned}$$

38 _____

39. $\frac{3}{5}(15t-35)+3t=\frac{-2}{3}(9t-12)+4$

$$\begin{aligned}9t-21+3t &= -6t+8+4 \\ 12t-21 &= -6t+12 \\ 12t+6t &= 12+21 \\ \frac{18t}{18} &= \frac{33}{18} \\ t &= 1\frac{5}{6}\end{aligned}$$

39 _____

$$40. 8(2d-5)+11=13d+8$$

$$16d - 40 + 11 = 13d + 8$$

$$16d - 29 = 13d + 8$$

$$16d - 13d = 8 + 29$$

$$3d = 37$$

$$d = 12\frac{1}{3}$$

$$40 \quad \underline{d = 12\frac{1}{3}}$$

$$41. \frac{2}{7}(28-21r)+3r=11r-(-7)$$

$$8 - 6r + 3r = 11r + 7$$

$$8 - 3r = 11r + 7$$

$$8 - 7 = 11r + 3r$$

$$1 = 14r$$

$$\frac{1}{14} = r$$

$$41 \quad \underline{\frac{1}{14} = r}$$

$$42. 5(3a-2) = \frac{3}{4}(16a+20)$$

$$15a - 10 = 12a + 15$$

$$15a - 12a = 15 + 10$$

$$\frac{3a}{3} = \frac{25}{3}$$

$$a = 8\frac{1}{3}$$

$$42 \quad \underline{a = 8\frac{1}{3}}$$

Solve each word problem, put final answer in box

43. Find three consecutive odd integers whose sum is (-21). Find the three integers.

$$\text{FIRST: } 2n+1$$

$$\text{SECOND: } 2n+3$$

$$\text{THIRD: } 2n+5$$

$$\text{FIRST} + \text{SECOND} + \text{THIRD} = -21$$

$$6n + 9 = -21$$

$$6n = -21 - 9$$

$$\frac{6n}{6} = \frac{-30}{6}$$

$$n = -5$$

$$\text{FIRST} = -9$$

$$\text{SECOND} = -7$$

$$\text{THIRD} = -5$$

44. Find three consecutive even integers whose sum is 138. Find the three integers.

$$\text{FIRST: } 2n$$

$$\text{SECOND: } 2n+2$$

$$\text{THIRD: } 2n+4$$

$$\text{FIRST} + \text{SECOND} + \text{THIRD} = 138$$

$$6n + 6 = 138$$

$$6n = 138 - 6$$

$$6n = 132$$

$$n = 22$$

$$\text{FIRST: } 44$$

$$\text{SECOND: } 46$$

$$\text{THIRD: } 48$$

45. A number increased by five times the difference of three and the twice number, is equal to seventeen less than, seven times that number. Find the number.

NUMBER: w

$$w + 5(3 - 2w) = 7w - 17$$

$$w + 15 - 10w = 7w - 17$$

$$15 - 9w = 7w - 17$$

$$15 + 17 = 7w + 9w$$

$$32 = 16w$$

$$w = 2$$

46. Find four consecutive odd integers whose sum is 72. Find the four integers.

FIRST: $2n+1$

SECOND: $2n+3$

THIRD: $2n+5$

FOURTH: $2n+7$

$$\text{FIRST} + \text{SECOND} + \text{THIRD} + \text{FOURTH} = 72$$

$$8n + 16 = 72$$

$$8n = 72 - 16$$

$$8n = 56$$

$$n = 7$$

FIRST: 15

SECOND: 17

THIRD: 19

FOURTH: 21

Simplify

47. $5 - (-8) - 11 =$

$$5 + 8 - 11$$

$$2$$

47. 2

48. $-4 \cdot -3 \cdot 2 \cdot 9 =$

$$12 \cdot 2 \cdot 9$$

$$216$$

48. 216

49. $-3\frac{2}{3} + -7\frac{1}{2} - -2\frac{1}{3} + 5\frac{3}{4} =$

$$-3 - 7 + 2 + 5$$

$$\frac{-8 - 6 + 4 + 9}{12}$$

$$= -3\frac{1}{12} = -3\frac{1}{12}$$

49. $-3\frac{1}{12}$

50. $-2\frac{1}{3} \cdot 3\frac{3}{4} \div 2\frac{1}{3} =$

$$-\frac{7}{3} \cdot \frac{15}{4} \cdot \frac{3}{7} = -3\frac{3}{4}$$

50. $-3\frac{3}{4}$

Function notation

$$f(x) = 3x - 8$$

$$g(x) = x^2 - 9$$

$$h(x) = x^2 - 3x + 5$$

51. $f(-1) = 3[-1] - 8 = \boxed{-11}$

51. -11

52. $g(2) + f(3) = -5 + 1 = \boxed{-4}$

$$g(2) = 2^2 - 9 = -5$$

52. -4

53. $h(5) = 5^2 - 3(5) + 5 = 25 - 15 + 5 = \boxed{15}$

$$f(3) = 3(3) - 8 = 1$$

53. 15

54. $f(1) + g(3) = \boxed{15}$

54. -5

$$f(1) = 3(1) - 8 = -5$$

$$g(3) = 9 - 9 = 0$$

$$-5 + 0 = \boxed{-5}$$

Function notation

$f(x) = 5x - 2$

$g(x) = x^2 + 1$

$h(x) = |x - 11|$

$w(x) = 3x + 4$

$$55. f(p) = \boxed{5p - 2}$$

$$h(0) = |0 - 11| = 11$$

$$55. \underline{5p - 2}$$

$$56. h(h(h(0)))$$

$$h(11) = |11 - 11| = 0$$

$$56. \underline{11}$$

$$57. h(5)$$

$$h(5) = |5 - 11| = 6$$

$$57. \underline{6}$$

$$58. f(m+5) + w(2m+7) + f(3m+1)$$

$$58. \underline{26m + 51}$$

$$5[m+5] - 2 + 3[2m+7] + 4 + 5[3m+1] - 2$$

$$\underline{5m+25-2} + \underline{6m+21+4} + \underline{15m+5-2}$$

$$26m + 51$$

Distribute and Combine Like Terms

$$59. -10 + 5(3k+4) - 2(5k-9) - 12k$$

$$\underline{-10 + 15k + 20} \quad \underline{-10k + 18} \quad \underline{-12k}$$

$$-7k + 28$$

$$59. \underline{-7k + 28}$$

$$60. 5(2x+7) - 2(5x-1)$$

$$10x + 35 - 10x + 2$$

$$37$$

$$60. \underline{37}$$

Solve each equation

$$61. \frac{2}{7}(21 - 35m) + 2m = 7m - (-6)$$

$$6 - 10m + 2m = 7m + 6$$

$$6 - 8m = 7m + 6$$

$$6 - 6 = 7m + 8m$$

$$0 = 15m$$

$$0 = m$$

$$61. \underline{0 = m}$$

$$62. \left[\frac{2}{3}n + \frac{4}{5} = \frac{1}{2}n - \frac{3}{5} \right] 30$$

$$20n + 24 = 15n - 18$$

$$20n - 15n = -18 - 24$$

$$\frac{5n}{5} = \frac{42}{5}$$

$$n = 8\frac{2}{5}$$

$$62. \underline{n = 8\frac{2}{5}}$$

$$63. \left[\frac{1}{2}z - \frac{2}{3}(4z+1) = \frac{1}{2} - \frac{3}{4}(2z-3) \right] 12$$

$$63. \underline{-5\frac{1}{8} = z}$$

hint: remember that if one were to multiply the entire equation by some value, what is in the parentheses is shielded.

$$6z - 8(4z+1) = 6 - 9(2z-3)$$

$$6z - 32z - 8 = 6 - 18z + 27$$

$$-26z - 8 = 33 - 18z$$

$$-8 - 33 = -18z + 26z$$

$$-41 = 8z$$

$$-\frac{41}{8} = \frac{8z}{8}$$

$$-5\frac{1}{8} = z$$

$$67.] \quad \frac{3}{7}(21y-14) - \frac{2}{9}(27y-81) = \frac{3y+2}{2} - \frac{2y-1}{4} + \frac{4y+3}{5} \quad : \text{EXPAND LEFTHAND SIDE}$$

$$9y-6-6y+18 = \frac{3y+2}{2} - \frac{2y-1}{4} + \frac{4y+3}{5} \quad : \text{COMBINE LIKE TERMS}$$

$$\frac{3y+12}{1} = \frac{3y+2}{2} - \frac{2y-1}{4} + \frac{4y+3}{5} \quad : \text{CONSIDER L.H.S. LIKE A FRACTION}$$

$$20 \left[\frac{3y+12}{1} = \frac{3y+2}{2} - \frac{2y-1}{4} + \frac{4y+3}{5} \right] \quad : \text{MULTIPLY BY COMMON DENOMINATOR}$$

$$20(3y+12) = 10(3y+2) - 5(2y-1) + 4(4y+3) \quad : \text{BRING DOWN NUMERATOR'S UNCHANGED, THEN DISTRIBUTE.}$$

$$60y + 240 = 30y + 20 - 10y + 5 + 16y + 12$$

$$60y + 240 = 36y + 37$$

: COMBINE LIKE TERMS

$$60y - 36y = 37 - 240$$

: MOVE VARIABLES TO ONE SIDE OF EQUATION, CONSTANTS TO OTHER

$$\frac{24y}{24} = \frac{-203}{24}$$

$$y = -8 \frac{11}{24}$$