

NAME _____

Simplify

#1 $\sqrt{108}$

#1 _____

#2 $\sqrt{125}$

#2 _____

#3 $\sqrt{20A^2B^3}$

#3 _____

#4 $\sqrt{27x^3y}$

#4 _____

#5 $\sqrt{\frac{5}{3}}$

#5 _____

#6 $\sqrt{\frac{4}{7}}$

#6 _____

#7 $\sqrt{\frac{147}{3}}$

#7 _____

#8 $\frac{2\sqrt{3}}{3-\sqrt{5}}$

#8 _____

#9 $\frac{3}{2+\sqrt{4}}$

#9 _____

#10 $8\sqrt{27} - 5\sqrt{12} + 2\sqrt{75}$

#10 _____

#11 $\sqrt{5} - 6\sqrt{20}$

#11 _____

#12 $3\sqrt{18} - 2\sqrt{50} + 6\sqrt{12}$

#12 _____

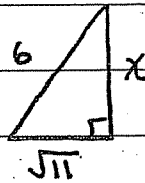
PYTHAGOREAN THEOREM

#13 A=

#13



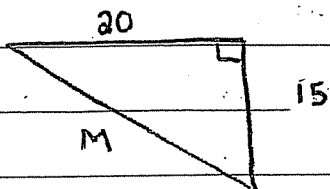
#14



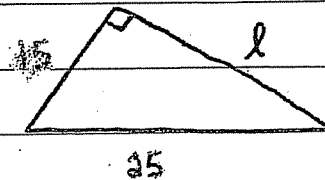
#14 x=

#15 M=

#15



#16



#16 l=

$$\#1 \quad \sqrt{108}$$

$$\sqrt{2^2 \cdot 3^2 \cdot 3}$$

$$\textcircled{6\sqrt{3}}$$

$$2 \overline{)108}$$

$$2 \overline{)54}$$

$$3 \overline{)27}$$

$$3 \overline{)9}$$

$$3$$

$$\#2 \quad \sqrt{125}$$

$$\sqrt{5^2 \cdot 5}$$

$$\textcircled{5\sqrt{5}}$$

$$5 \overline{)125}$$

$$5 \overline{)25}$$

$$5$$

$$\#3 \quad \sqrt{20A^2B^3}$$

$$\sqrt{2^2 \cdot 5 \cdot A^2 \cdot B^2 \cdot B}$$

$$2 \overline{)20}$$

$$2 \overline{)10}$$

$$5$$

$$\textcircled{2|AB|\sqrt{5B}}$$

$$\#4 \quad \sqrt{27x^3y}$$

$$\sqrt{3^2 \cdot 3 \cdot x^2 \cdot xy}$$

$$3 \overline{)27}$$

$$3 \overline{)9}$$

$$3$$

$$\textcircled{3|x|\sqrt{3xy}}$$

$$\#5 \quad \sqrt{\frac{5}{3}}$$

$$\frac{\sqrt{5} \cdot \sqrt{3}}{\sqrt{3} \cdot \sqrt{3}}$$

$$\textcircled{\frac{\sqrt{15}}{3}}$$

$$\#6 \quad \sqrt{\frac{4}{7}}$$

$$\frac{\sqrt{4}}{\sqrt{7}} = \frac{2}{\sqrt{7}} \cdot \frac{\sqrt{7}}{\sqrt{7}}$$

$$\textcircled{\frac{2\sqrt{7}}{7}}$$

$$\#7 \quad \frac{\sqrt{147}}{\sqrt{3}} = \sqrt{49}$$

$$\textcircled{= 7}$$

$$\#8 \quad \frac{2\sqrt{3}}{3-\sqrt{5}}$$

$$\frac{2\sqrt{3}}{3-\sqrt{5}} \cdot \frac{3+\sqrt{5}}{3+\sqrt{5}}$$

$$\frac{2\sqrt{3}(3+\sqrt{5})}{9-5}$$

$$\frac{2\sqrt{3}(3+\sqrt{5})}{4} \quad ; \text{REDUCE 2 AND 4}$$

$$\frac{\sqrt{3}(3+\sqrt{5})}{4} \quad ; \text{DISTRIBUTE}$$

$$\textcircled{\frac{3\sqrt{3} + \sqrt{15}}{4}}$$

$$\#9 \quad \frac{3}{2+\sqrt{4}}$$

$$\frac{3}{2+2}$$

$$: \sqrt{4} = 2$$

$$\textcircled{\frac{3}{4}}$$

$$\#10 \quad 8\sqrt{27} - 5\sqrt{12} + 2\sqrt{75}$$

$$8\sqrt{3^2 \cdot 3} - 5\sqrt{2^2 \cdot 3} + 2\sqrt{5^2 \cdot 3}$$

$$24\sqrt{3} - 10\sqrt{3} + 10\sqrt{3}$$

$$\textcircled{24\sqrt{3}}$$

$$\#11 \quad \sqrt{5} - 6\sqrt{20}$$

$$\sqrt{5} - 6\sqrt{2^2 \cdot 5}$$

$$\sqrt{5} - 12\sqrt{5}$$

$$\textcircled{-11\sqrt{5}}$$

#12 $3\sqrt{18} - 2\sqrt{50} + 6\sqrt{12}$
 $3\sqrt{3^2 \cdot 2} - 2\sqrt{5^2 \cdot 2} + 6\sqrt{2^2 \cdot 3}$
 $9\sqrt{2} - 10\sqrt{2} + 12\sqrt{3}$

$-\sqrt{2} + 12\sqrt{3}$

#13

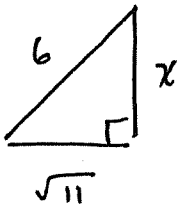


$l^2 + l^2 = h^2$
 $(\sqrt{23})^2 + (11)^2 = h^2$

$A = 12$

$23 + 121 = h^2$
 $144 = h^2$
 $12 = h$

#14



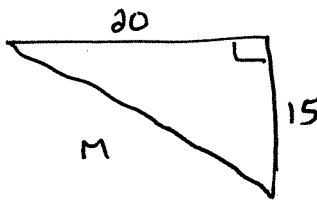
$l^2 + l^2 = h^2$
 $(\sqrt{11})^2 + x^2 = 6^2$

$11 + x^2 = 36$

$x^2 = 25$

$x = 5$

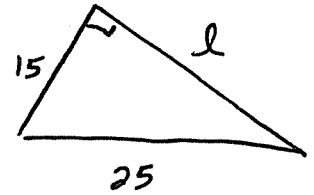
#15



$3(5) : 4(5) : 5(5)$

$m = 25$

#16



$3(5) : 4(5) : 5(5)$

$l = 20$

#17

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

#18

$\frac{4 \pm \sqrt{16 - 4(4)(-3)}}{2(4)}$

$\frac{4 \pm \sqrt{16 + 48}}{8}$

$\frac{4 \pm \sqrt{64}}{8}$

$\frac{4 \pm 8}{8}$

$\frac{4-8}{8}, \frac{4+8}{8}$

$-\frac{4}{8}, \frac{12}{8}$

$\left\{-\frac{1}{2}, \frac{3}{2}\right\}$

#19

$\frac{-21 \pm \sqrt{441 - 4(2)(40)}}{2(2)}$

$\frac{-21 \pm \sqrt{441 - 320}}{4}$

$\frac{-21 \pm \sqrt{121}}{4}$

$\frac{-21 \pm 11}{4}$

$\frac{-21-11}{4}, \frac{-21+11}{4}$

$-\frac{32}{4}, -\frac{10}{4}$

$\{-8, -2\frac{1}{2}\}$

#20

$$\sqrt{m+2} = m-4$$

$$[\sqrt{m+2}]^2 = [m-4]^2$$

$$\begin{array}{r} m+2 = m^2-8m+16 \\ -m-2 \quad \quad -m-2 \\ \hline 0 = m^2-9m+14 \end{array}$$

$$0 = (m-7)(m-2)$$

CHECK RESULTS $\Rightarrow m=7 \quad m=2$

$$m=7$$

#21

$$\sqrt{4x+1} = 3$$

$$[\sqrt{4x+1}]^2 = 3^2$$

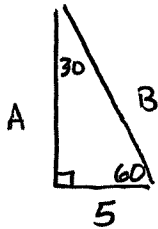
$$4x+1 = 9$$

$$4x = 8$$

CHECK RESULT $\Rightarrow x=2$

$$x=2$$

#22



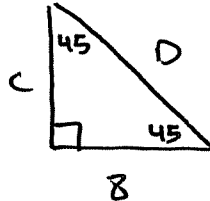
SL: LL: H

$$1: \sqrt{3}: 2$$

$$5: 5\sqrt{3}: 10$$

$$\begin{array}{l} A = 5\sqrt{3} \\ B = 10 \end{array}$$

#23



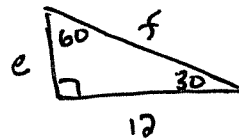
L: L: H

$$1: 1: \sqrt{2}$$

$$8: 8: 8\sqrt{2}$$

$$\begin{array}{l} C = 8 \\ D = 8\sqrt{2} \end{array}$$

#24



SL: LL: H

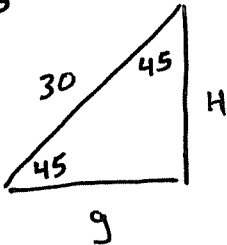
$$1: \sqrt{3}: 2$$

$$4\sqrt{3}: 12: 8\sqrt{3}$$

$$\begin{array}{l} e = 4\sqrt{3} \\ f = 8\sqrt{3} \end{array}$$

$$\begin{aligned} SL &= \frac{12}{\sqrt{3}} \\ &= \frac{12\sqrt{3}}{\sqrt{3}\sqrt{3}} \\ &= \frac{12\sqrt{3}}{3} = 4\sqrt{3} \end{aligned}$$

#25



L: L: H

$$1: 1: \sqrt{2}$$

$$15\sqrt{2}: 15\sqrt{2}: 30$$

$$\begin{array}{l} g = 15\sqrt{2} \\ H = 15\sqrt{2} \end{array}$$

$$\begin{aligned} L &= \frac{30}{\sqrt{2}} \\ &= \frac{30\sqrt{2}}{\sqrt{2}\sqrt{2}} \\ &= \frac{30\sqrt{2}}{2} \\ &= 15\sqrt{2} \end{aligned}$$

DISTANCE FORMULA

$$d = \sqrt{(\Delta x)^2 + (\Delta y)^2}$$

$$\#26 \quad \begin{matrix} \Delta x & x & y & \Delta y \\ -3 & (3, 0) & & 4 \\ \Delta x & (0, 4) & & \Delta x \end{matrix}$$

$$\begin{aligned} d &= \sqrt{(-3)^2 + (4)^2} \\ &= \sqrt{9 + 16} \\ &= \sqrt{25} \\ &= 5 \end{aligned}$$

$$\#27 \quad \begin{matrix} \Delta x & x & y & \Delta y \\ 2\sqrt{5} & (2\sqrt{5}, 9) & & -6 \\ 2\sqrt{5} & (4\sqrt{5}, 3) & & -6 \end{matrix}$$

$$\begin{aligned} d &= \sqrt{(2\sqrt{5})^2 + (-6)^2} \\ &= \sqrt{4 \cdot 5 + 36} \\ &= \sqrt{20 + 36} \\ &= \sqrt{56} \\ &= \sqrt{2^2 \cdot 14} \\ &= 2\sqrt{14} \end{aligned}$$

$$\begin{array}{r} 2 \overline{)56} \\ 2 \overline{)28} \\ 2 \overline{)14} \\ \quad 7 \end{array}$$

$$\#28 \quad \begin{matrix} \Delta x & x & y & \Delta y \\ 6 & (5, -1) & & +8 \\ & (11, 7) & & \end{matrix}$$

$$\begin{aligned} d &= \sqrt{(\Delta x)^2 + (\Delta y)^2} \\ &= \sqrt{6^2 + 8^2} \\ &= \sqrt{36 + 64} \\ &= \sqrt{100} \\ &= 10 \end{aligned}$$

MID-POINT AVERAGE X AVERAGE Y

$$\frac{y_1 + x_2}{2}, \quad \frac{y_1 + y_2}{2}$$

#29	$(7\frac{1}{2}, 8)$ $(4\frac{1}{2}, 7)$ $\frac{12}{2}, \frac{15}{2}$ MP $(6, 7\frac{1}{2})$	#30	$(3, 5)$ $(3, 2)$ $\frac{6}{2}, \frac{7}{2}$ MP $(3, 3\frac{1}{2})$	#31	$(2, 13)$ $(9, 1)$ $\frac{11}{2}, \frac{14}{2}$ MP $(5\frac{1}{2}, 7)$
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SLOPE $\frac{\Delta y}{\Delta x}$ (ALWAYS REPORT AS IMPROPER FRACTION)

$$\boxed{A} \quad \begin{matrix} \Delta x & x & y & \Delta y \\ -1 & (3, 7) & & -10 \\ & (2, -3) & & \end{matrix}$$

$$m = \frac{\Delta y}{\Delta x} = \frac{-10}{-1} = \frac{10}{1}$$

$$\boxed{B} \quad \begin{matrix} \Delta x & x & y & \Delta y \\ -8 & (3, 2) & & +9 \\ & (-5, 11) & & \end{matrix}$$

$$m = \frac{\Delta y}{\Delta x} = \frac{9}{-8} = \frac{-9}{8}$$

$$\boxed{C} \quad \begin{matrix} \Delta x & x & y & \Delta y \\ +5 & (-2, 7) & & -3 \\ & (3, 4) & & \end{matrix}$$

$$m = \frac{-3}{5}$$