

| Property / Identity                    | Definition   | Examples   |
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| <b>Additive Identity</b>               | When the sum of a number and zero is taken, the result is that the number is unchanged.  | 1) $3 + 0 = 3$<br>2) $R + 0 = R$<br>3) $-\frac{5}{7} = -\frac{5}{7} + 0$   |
| <b>Additive Inverse</b>                | Adding opposites produces a result that is the additive identity "0"   | 1) $-A + A = 0$<br>2) $-6 + 6 = 0$<br>3) $1.342 - 1.342 = 0$   |
| <b>Multiplicative Identity</b>         | When the product of a number and one is taken, the result is that the number is unchanged.   | 1) $11 \cdot 1 = 11$<br>2) $ABC = 1ABC$<br>3) $1 \cdot \left(-\frac{4}{5}\right) = -\frac{4}{5}$   |
| <b>Multiplicative Inverse</b>          | Multiplying reciprocals produces a result that is the multiplicative identity "1"  | 1) $\frac{3}{4} \cdot \left(\frac{4}{3}\right) = 1$<br>2) $B \cdot \left(\frac{1}{B}\right) = 1$<br>3) $1 = \frac{-1}{17} \cdot \frac{-17}{1}$   |
| <b>Multiplicative Property of Zero</b> | Any number multiplied by zero will produce an answer of zero.  | 1) $5 \cdot 7 \cdot 0 \cdot 3 = 0$<br>2) $0 = 0 \cdot W$<br>3) $-\frac{4}{5} \cdot 0 = 0$  |
| <b>Reflexive Property</b>              | This occurs when an exact copy or duplicate of an expression or equation is created.   | 1) $5x - 3 = 5x - 3$<br>2) $11y + 2 = 11y + 2$<br>3) $5a^2 - 2a + 3 = 5a^2 - 2a + 3$   |
| <b>Transitive Property</b>             | Two valid statements will initially be given, one can then logically arrive at a third valid statement by passing on the shared trait. | 1) If Mike is taller than Troy, and Troy is taller than Peter, then Mike is taller than Peter.<br>2) If $a = b$ , and $b = c$ , then $a = c$ .<br>3) If $2(5) = 7 + 3$ & $7 + 3 = 10$ , then $2(5) = 10$ |
| <b>Substitution Property</b>           | This is the catch 22, If no other property or identity describes the scenario this "replacement property" should be used.              | 1) $2(4 + 3) = 2(7)$<br>2) $5(7) - 11 = 35 - 11$<br>3) $11^2 + [6 - 3] = 121 + 3$  |

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| <b>Symmetric Property</b>                                | This is when the R.H.S. and L.H.S. of an equation are switched, but the individual terms are left in the same order.                   | 1) If $A - 7 = B + 4$ , then $B + 4 = A - 7$<br>2) If $y + 2 = x^2 - 4x + 9$ , then $x^2 - 4x + 9 = y + 2$<br>3) If $w = 3f - 7$ , then $3f - 7 = w$ |
| <b>Associative Property for Addition</b>                 | When a series of terms are being added together one can regroup the terms using parentheses but the end result is left unchanged.      | 1) $5 + (8 + 9) = (5 + 8) + 9$<br>2) $(a + b) + c = a + b + c$<br>3) $1 + (2 + 3) + 1 = (1 + 2 + 3) + 1$   |
| <b>Associative Property for Multiplication</b>           | When a series of terms are being multiplied together one can regroup the terms using parentheses but the end result is left unchanged. | 1) $(de)f = d(ef)$<br>2) $7 \cdot (3 \cdot 4) \cdot 2 = 7 \cdot [(3 \cdot 4) \cdot 2]$<br>3) $c(de)f = (cd)(ef)$                                     |
| <b>Commutative Property for Addition</b>                 | When a series of terms are being added together one can rearrange the terms without effecting the end result.                          | 1) $7 + 2 + 5 = 2 + 5 + 7$<br>2) $ab + 5 + c = 5 + ab + c$<br>3) $9 + 7 + 6 = 7 + 6 + 9$   |
| <b>Commutative Property for Multiplication</b>           | When a series of terms are being multiplied together one can rearrange the terms without effecting the end result.                     | 1) $abc = bca = cba$<br>2) $cd - 7 = dc - 7$<br>3) $2(5)(9) = 2(9)(5) = 9(2)(5)$   |
| <b>Distributive Property from right over addition</b>    | When a value on the right side of a set of parentheses, is multiplied across terms separated by an operation of addition.              | 1) $(11x + 3)2 = 11x \cdot 2 + 3 \cdot 2$<br>2) $(3w + 7)5 = 15w + 35$<br>3) $(2m + 1)9 = 18m + 9$   |
| <b>Distributive Property from right over subtraction</b> | When a value on the right side of a set of parentheses, is multiplied across terms separated by an operation of subtraction.           | 1) $(7x - 3)6 = 7x \cdot 6 - 3 \cdot 6$<br>2) $(4p - 5)2 = 8p - 10$<br>3) $(2y - 3)11 = 22y - 33$  |
| <b>Distributive Property from left over addition</b>     | When a value on the left side of a set of parentheses, is multiplied across terms separated by an operation of addition.               | 1) $3(2m + 5) = 3 \cdot 2m + 3 \cdot 5$<br>2) $7(2x + 3) = 14x + 21$<br>3) $5(6t + 1) = 30t + 5$   |
| <b>Distributive Property from left over subtraction</b>  | When a value on the left side of a set of parentheses, is multiplied across terms separated by an operation of subtraction.            | 1) $7(2k - 3) = 7 \cdot 2k - 7 \cdot 3$<br>2) $8(3w - 9) = 24w - 72$<br>3) $\frac{2}{3}(6m - 9) = 4m - 6$  |

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| <b>Closure Property</b> | This is essentially a containment process where, given a set of numbers and an operation, the results create other numbers within the set.  | {Odd Integers}; multiplication<br>1) $5 \cdot 7 = 35$<br>2) $-3 \cdot 11 = -33$<br>3) odd(odd) always equals an odd therefore, the operation on the set is considered <b>closed</b> .   |
|                         | Note: One counter example, the example that demonstrates that a result of using the operator does not produce a number within the set, is all that is needed to show the operation is not closed. | {Odd Integers}; addition<br>1) $5 + 3 = 8$<br>2) $-11 + 13 = 2$<br>3) odd + (odd) never equals odd therefore, the operation on the set is considered <b>not closed</b> .  |
|                         | Note: Many times it will prove helpful to use the same two numbers when testing for closure but reverse the order in the trials.  | {Whole Numbers}; subtraction<br>1) $11 - 5 = 6$<br>2) $5 - 11 = -6$<br>3) Whole - Whole sometimes equals a whole number therefore, the operation on the set is considered <b>not closed</b> .   |
|                         |   | {Integers}; division<br>1) $30 \div 6 = 5$<br>2) $6 \div 30 = \frac{1}{5}$<br>3) Integer $\div$ Integer sometimes equals an integer number therefore, the operation on the set is considered <b>not closed</b> .  |
|                         | Note: Here is an example of a more complex operation where multiple steps are involved in the process. As mentioned earlier reverse the order of the numbers when checking for closure.           | {Even Numbers}; $a^2 - a \cdot b$<br>1) $4^2 - 4 \cdot 6 = -8$<br>2) $6^2 - 6 \cdot 4 = 12$<br>3) $(-2)^2 - (-2) \cdot 20 = 44$<br>4) The results appear to remain within the original set of numbers so the operation on the set is considered <b>closed</b> . |