

Conceptual Questions Some of these items will be on the actual test

1. What is the first step when adding or subtracting mixed numbers or fractions?

Find a **common denominator**

2. What is the definition of “Rational Numbers”?

Any number that can be written as a **fraction** and when **written as a decimal** will either **repeat** or **terminate**

3. What is the first step when multiplying or dividing mixed numbers?

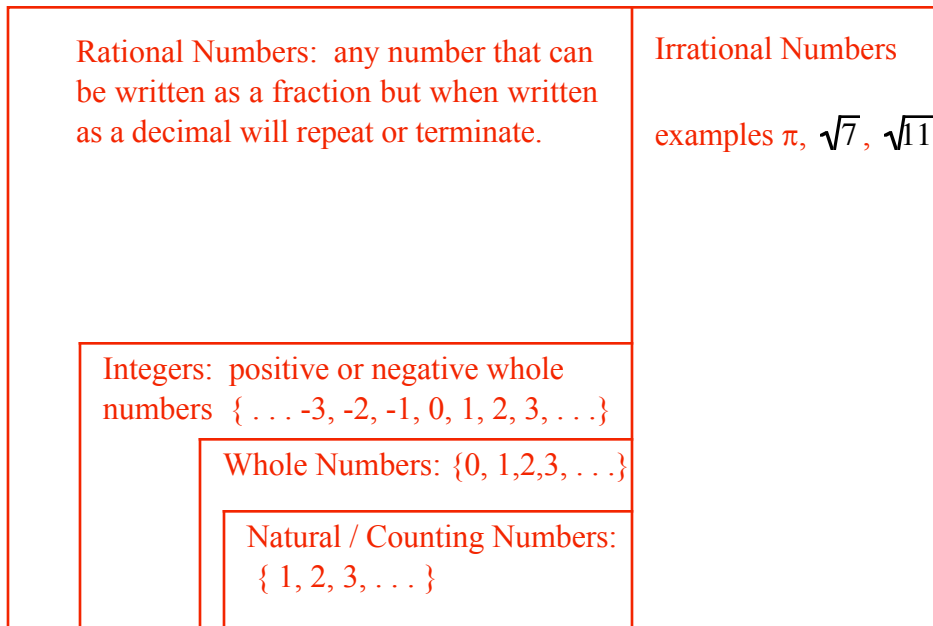
Create **Improper Fractions**

4. What is the definition of “Integer Numbers”?

Any number that is a **positive** or **negative whole number** falls into this number set.

5. Explain the “Universe of Numbers” by illustrating the various number sets and how each is related.

Real Numbers - Any number that one can write



5.1 Provide an example of each **number set**.

Natural / Counting Numbers - { 1, 2, 3, ... }

Whole Numbers - {0, 1,2,3, ... }

Integer Numbers - { ... -3, -2, -1, 0, 1, 2, 3, ... }

Rational Numbers - any number that can

be written as a fraction but when written as a decimal will repeat or terminate.

Irrational Numbers -any number that when written as a decimal will **not** repeat or terminate

Real Numbers -Any number that one can write

6. Illustrate the borrowing idea with this problem.

$$\begin{array}{r}
 25\frac{1}{3} - 20\frac{3}{4} \\
 25 - 20 \quad | \quad 1/3 - 3/4 \\
 5 \quad \quad | \quad 4/12 - 9/12 \\
 5 \quad \quad | \quad -5/12 \\
 4 \quad 12/12 \quad | \quad -5/12 \\
 4 \quad \quad \quad | \quad 7/12
 \end{array}$$

: Work whole with whole and part with part

: signs do not match so borrow

: equivalent statement $5 = 4 \quad 12/12$

: then work part with part so signs on mixed number match

Knowing the Squares (Should take less than a minute to do entire section)

- | | |
|-------------|---------------|
| 1. $13^2 =$ | 1. <u>169</u> |
| 2. $16^2 =$ | 2. <u>256</u> |
| 3. $18^2 =$ | 3. <u>324</u> |
| 4. $19^2 =$ | 4. <u>361</u> |
| 5. $21^2 =$ | 5. <u>441</u> |
| 6. $22^2 =$ | 6. <u>484</u> |
| 7. $23^2 =$ | 7. <u>529</u> |
| 8. $25^2 =$ | 8. <u>625</u> |

Add and Subtracting Integers

- | | |
|--|----------|
| 1. $25 + 14 - 11$
39 - 11
28 | 1. _____ |
| 2. $-17 + (-13) + 3$
-30 + 3
-27 | 2. _____ |
| 3. $7 - (-5) - 19$
12 - 19
-7 | 3. _____ |

Multiplying and Dividing Integers

- | | |
|--|----------|
| 4. $(-12)(5) \div (-6)$
-60 / -6
10 | 4. _____ |
| 5. $(-4)(-3) \div 2(-6)$
12 / 2 (-6)
6 (-6)
-36 | 5. _____ |
| 6. $-5 \cdot -3 \cdot 0 \cdot 7$
15 (0) (7)
0 (7)
0 | 6. _____ |

Addind and Subtracting Rationals

7. $-8\frac{1}{4} + 12\frac{2}{5} - 3\frac{7}{10}$

$$\begin{array}{r|l} -8 + 12 - 3 & -1/4 + 2/5 - 7/10 \\ 1 & -5/20 + 8/20 - 14/20 \\ 1 & -11/20 \\ 20/20 & -11/20 \\ & 9/20 \end{array}$$

7. _____

: Work whole with whole and part with part

: signs do not match so borrow

: equivalent statement $1 = 20/20$

: then work part with part so signs on mixed number match

8. $-4\frac{2}{5} - \left(-4\frac{1}{2}\right) - 2\frac{3}{5}$

$$\begin{array}{r|l} -4 + 4 - 2 & -2/5 + 1/2 - 3/5 \\ -2 & -4/10 + 5/10 - 6/10 \\ -2 & -5/10 \\ -2 & 1/2 \end{array}$$

8. _____

: Work whole with whole and part with part

: signs match so no need to borrow

: just reduce fraction

Multiplying and Dividing Rationals

9. $\left(-\frac{1}{5}\right) \div \frac{2}{15} \cdot \left(-1\frac{1}{7}\right)$

$$\begin{array}{l} -1/5 \circ 15/2 \circ -8/7 \\ -1/1 \circ 3/1 \circ -4/7 \\ 12/7 \\ 1 \ 5/7 \end{array}$$

9. _____

: get improper fractions and reciprocate any divisors

: reduce any numerator with any denominator

: just reduce fraction

10. $\left(-4\frac{2}{3}\right) \div \left(-3\frac{1}{2}\right) \cdot 1\frac{1}{5}$

$$\begin{array}{l} -14/3 \div -7/2 \circ 6/5 \\ -14/3 \circ -2/7 \circ 6/5 \\ -2/1 \circ 2/1 \circ -2/5 \\ 8/5 \\ 1 \ 3/5 \end{array}$$

10. _____

: get improper fractions

: reciprocate any divisors

: reduce any numerator with any denominator

: just reduce fraction

11. $\frac{8}{15} \div \left(-\frac{2}{5}\right) \div \left(-\frac{1}{2}\right)$

$$\begin{array}{l} 8/15 \circ -5/2 \circ -2/1 \\ 8/3 \circ -1/1 \circ -1/1 \\ 8/3 \\ 2 \ 2/3 \end{array}$$

11. _____

: reciprocate any divisors

: reduce any numerator with any denominator

: just reduce fraction

Order of Operations

$$\begin{aligned} & 2[(16 \div 8) - (-2)] + 4 \\ & 2[(2) - (-2)] + 4 \\ 12. & 2[2 + 2] + 4 \\ & 2[4] + 4 \\ & 8 + 4 \\ & 12 \end{aligned}$$

$$\begin{aligned} & \frac{2}{3}[8(2-5)^2 + 3 \cdot 2] \\ & \frac{2}{3}[8(-3)^2 + 3 \cdot 2] \\ 13. & \frac{2}{3}[8 \cdot 9 + 6] \\ & \frac{2}{3}[72 + 6] \\ & \frac{2}{3}[78] \\ & 52 \end{aligned}$$

Order of Operations

$$\begin{aligned} & 6[3 - (-4 + 2) \div 2] \\ & 6[3 - (-2) \div 2] \\ 14. & 6[3 - -1] \\ & 6[3 + 1] \\ & 6[4] \\ & 24 \end{aligned}$$

$$\begin{aligned} & 9\left[\left(\frac{5}{8} - \frac{1}{4}\right) \cdot \frac{1}{9} \div \frac{3}{4}\right] \\ & 9\left[\left(\frac{5}{8} - \frac{2}{8}\right) \cdot \frac{1}{9} \cdot \frac{4}{3}\right] \\ 15. & 9\left[\left(\frac{3}{8}\right) \cdot \frac{1}{9} \cdot \frac{4}{3}\right] \\ & 9\left[\left(\frac{1}{2}\right) \cdot \frac{1}{9} \cdot \frac{1}{1}\right] \\ & \frac{9}{1}\left[\frac{1}{18}\right] \\ & \frac{1}{2} \end{aligned}$$

(Show all work since answers given)

$$\left(-\frac{3}{5}\right)^2 - \frac{3}{5} \cdot 2\frac{3}{5} + \frac{7}{10} = -\frac{1}{2}$$

$$\left(\frac{9}{25}\right) - \frac{3}{5} \cdot \frac{13}{5} + \frac{7}{10}$$

$$\left(\frac{9}{25}\right) - \frac{39}{25} + \frac{7}{10}$$

16. $-\frac{30}{25} + \frac{7}{10}$

$$-\frac{6}{5} + \frac{7}{10}$$

$$-\frac{12}{10} + \frac{7}{10}$$

$$-\frac{5}{10}$$

$$-\frac{1}{2}$$

$$\left[\frac{1}{6} \div \frac{5}{9} - \left(\frac{1}{5}\right)^2\right] - \frac{7}{10} = -\frac{11}{25}$$

$$\left[\frac{1}{6} \cdot \frac{9}{5} - \frac{1}{25}\right] - \frac{7}{10}$$

$$\left[\frac{1}{2} \cdot \frac{3}{5} - \frac{1}{25}\right] - \frac{7}{10}$$

17. $\left[\frac{3}{10} - \frac{1}{25}\right] - \frac{7}{10}$

$$\left[\frac{15}{50} - \frac{2}{50}\right] - \frac{35}{50}$$

$$-\frac{22}{50}$$

$$-\frac{11}{25}$$

Exploring Patterns

A. 1, 2, 4, 8, 10, 20, 22,
x2 + 2

44 , 46 , 92

B. 33, 39, 40, 47, 48, 56, 57,
+6 +1 +7 +1 +8 +1 +9 +1 +10

66 , 67 , 77

C. 4, 7, 12, 19, 28, 39, 52,
+3 +5 +7 +9 +11 ...

67 , 84 , 103

D. 169, 196, 225, 256, 289, 324,
squares

361 , 400 , 441

E. 10, 8, 16, 18, 9, 6, 18, 21, 7, 3
-2, x 2, +2, ÷ 2, -3, x 3, +3, ÷ 3, -4, x 4, +4, ÷ 4

12 , 16 , 4

F. 80, 77, 76, 72, 71, 66, 65,
-3 -1 -4 -1 -5 -1 ...

59 , 58 , 51